

# Computer Simulation of the Dynamic Behavior of the Glutathione-Ascorbate Redox Cycle in Chloroplasts<sup>1</sup>[W]

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The glutathione-ascorbate redox pathway in chloroplasts is a complex network of spontaneous, photochemical, and enzymatic reactions for detoxifying hydrogen peroxide. This article presents a comprehensive sensitivity analysis of the system. A model has been constructed to simulate oxidative stress conditions, enabling steady-state concentrations of the metabolites involved in the pathway and photochemical and enzymatic fluxes to be calculated. The model includes an electron source whose flux is distributed among three competitive routes (photogeneration of  $O_2^-$ , photoreduction of  $NADP^+$  to NADPH, and photoreduction of monodehydroascorbate to ascorbate) and that allows the simulation of variations in NADPH concentration with time. Each enzyme considered is introduced in the model, taking into account its particular catalytic mechanism, including the inactivation of ascorbate peroxidase in the presence of low-ascorbate concentrations. Computer simulations pointed to the great sensitivity of the system to the ratio among fluxes corresponding to ascorbate and NADPH photoproduction and NADPH consumption by the Calvin cycle. Under oxidative stress conditions, the model shows a sequential depletion of antioxidant power in chloroplasts in the order NADPH, glutathione, ascorbate and their recovery in the reverse order. Decreasing levels of glutathione reductase, ascorbate peroxidase, and superoxide dismutase led to the irreversible photoinactivation of ascorbate peroxidase and the subsequent increase in hydrogen peroxide concentration, preceded by a maximum in dehydroascorbate reductase activity.

In plants, the main generation sites of reactive oxygen species (ROS) are the reaction centers of PSI and PSII in chloroplast thylakoids. Under steady-state conditions, the intracellular level of ROS is tightly buffered and controlled by detoxifying antioxidant systems formed of a network of enzymatic and non-enzymatic components (Noctor and Foyer, 1998; Mittler, 2002). Superoxide dismutase (superoxide:superoxide oxidoreductase [SOD]; EC 1.15.1.1) acts as the first line of defense against ROS by dismutating  $O_2^-$  to hydrogen peroxide ( $H_2O_2$ ) and  $O_2$ . In chloroplasts, the  $H_2O_2$  thus generated is reduced to water by ascorbate (ASC) catalyzed with L-ascorbate peroxidase (L-ascorbate:hydrogen peroxide oxidoreductase [APX]; EC 1.11.1.11). This is the first step of the so-called glutathione-ascorbate (GSH-ASC) cycle, also named the water-water cycle (Asada, 1999, 2006). Dehydroascorbate reductase (glutathione:dehydroascorbate oxidoreductase [DHAR]; EC 1.8.5.1), monodehydroascorbate reductase (NADH:monodehydroascorbate oxidoreductase [MDAR]; EC

1.6.5.4), and glutathione reductase (glutathione:NADP<sup>+</sup> oxidoreductase [GR]; EC 1.8.1.7) also participate in the pathway (Fig. 1), which uses ASC, GSH, and NADPH as electron donors (for an extensive review of the pathway, see Asada, 1999).

Numerous studies have been performed on the GSH-ASC cycle, and it is still a matter of intensive research (Noctor and Foyer, 1998; Asada, 1999, 2006). The computer modeling of metabolic systems is an increasingly used tool that has enhanced our understanding of the behavior of metabolic pathways. It was introduced to analyze pathways in chloroplasts in the early 1980s (Laisk and Walker, 1986; Hahn, 1987), and more recently, a very interesting paper has analyzed the network of redox reactions of the GSH-ASC cycle (Polle, 2001). The model was successfully used to simulate the functioning of the redox cycle in chloroplasts, making it possible to calculate steady-state concentrations of species and fluxes of steps involved in the reaction scheme proposed. However, the model has some limitations, such as the assumption of a constant NADPH concentration during the simulation time, the nonreduction of the  $NADP^+$  formed (leading to the erroneous accumulation of  $NADP^+$  in the chloroplast), and a constant  $O_2^-$  production rate during the simulation time. Furthermore, the fact that the kinetic behavior of the enzymes involved in the pathway was introduced with an identical equation, that corresponding to a ping-pong bi bi reaction mechanism (except SOD, which was treated as a bimolecular reaction), means that the model should be modified.

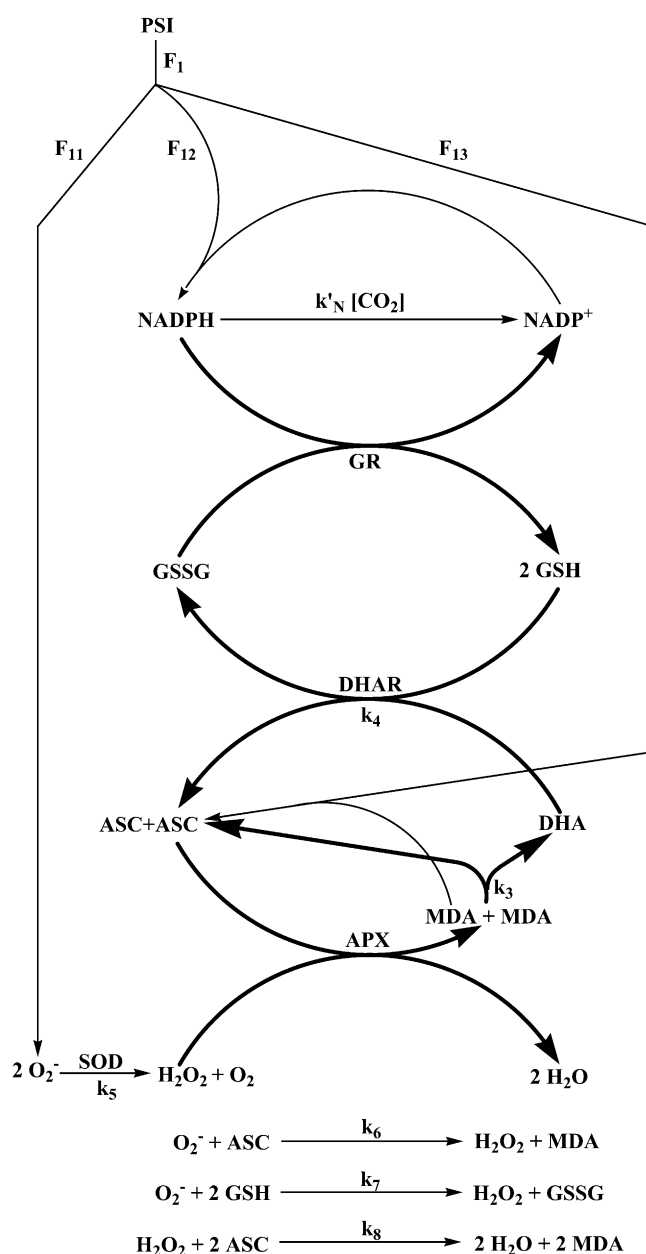
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**Figure 1.** Schematic representation of the model to simulate the dynamic behavior of the GSH-ASC pathway in chloroplasts.  $k_i$  values ( $i = 3-8$ ) are apparent bimolecular rate constants for the spontaneous steps included in the model.

The aim of this article was to extend the above approach in several aspects in an attempt to improve the model and to bring it closer to what occurs in reality. In this way, the model will allow a better scientific understanding of the spontaneous and enzymatic reactions involved in the pathway and may contribute to the prediction of results in the design of experiments. (1) The electron flux from PSI has been considered as being distributed among three competitive routes involving the photogeneration of  $\text{O}_2^-$  from  $\text{O}_2$ , the photoreduction of  $\text{NADP}^+$  to NADPH, and the photoreduction of monodehydroascorbate radicals (MDA)

to ASC. In this way,  $\text{NADP}^+$  is recycled to NADPH and the electron flux related to the production of  $\text{O}_2^-$  is changeable and dependent on the availability of NADPH and MDA, making the model much more flexible, since the three fluxes must be adapted to each other to respond to stress conditions. (2) Each enzymatic activity involved in the cycle has been introduced in the model, taking into account the particular catalytic mechanism of each enzyme. In addition, an inactivation step for APX in the presence of  $\text{H}_2\text{O}_2$  (Miyake et al., 2006) has been included along with a route for the de novo synthesis of the protein. This last step represents one of the main defense mechanisms of plants to mitigate oxidative stress, so the recovery of APX inactivated by an excess of  $\text{H}_2\text{O}_2$  can be simulated. (3) An additional step representing NADPH consumption in the Calvin cycle has been added, so that the competition between the NADPH consumed by the ROS-detoxifying pathway and the NADPH consumed by the Calvin cycle is included. (4) The model has been constructed based on the ordinary differential equations (ODE) system corresponding to the network of spontaneous and enzymatic steps involved in the cycle. Computer simulations have been performed by numerical integration of this set of ODE using the easily accessible software MATLAB. This software has several ODE solver routines for nonstiff and stiff (as in the present case) problems, so users can choose the best option for their specific problem.

## DESCRIPTION OF THE MODEL

The system being studied is depicted in Figure 1. There is a constant electron source in the model, PSI, whose flux is divided among three competitive routes: (1) the photoproduction of  $\text{O}_2^-$ ; (2) the photoreduction of  $\text{NADP}^+$ ; and (3) the photoreduction of MDA. The last two processes are ferredoxin (Fd) dependent, although Fd has not been introduced as a variable in the present model, and only electron fluxes have been considered. The same holds for the electron donor species involved in the photogeneration of  $\text{O}_2^-$  (in the same way,  $[\text{O}_2]$  and  $[\text{CO}_2]$  have also been considered constants). For the notation and definitions used for the fluxes, see Table I.  $F_{13}$  has been considered as directly proportional to  $[\text{MDA}]$ ,  $k_{13}$  being the proportionality constant. Factor 2 in  $F_{12}$  indicates the fact that the reduction of  $\text{NADP}^+$  to NADPH is a two-electron process.  $F_{11}$  is the remaining flux from PSI. In this way  $F_{11}$ ,  $F_{12}$ , and  $F_{13}$  are variable and dependent on the  $[\text{NADP}^+]$  and  $[\text{MDA}]$  present in chloroplasts. This imparts great flexibility to the model and a greater ability to study stress conditions in chloroplasts.

## Enzymes Involved in the Model

### SOD

The  $\text{O}_2^-$  photogenerated directly by the PSI complex is mainly disproportionated to  $\text{H}_2\text{O}_2$  and  $\text{O}_2$  catalyzed by SOD. This reaction has a 10,000-fold faster rate than

**Table I.** Notation and definitions of fluxes used in the present model

Notation	Definition	Mathematical Expression
$F_1$	Electron flow from PSI	$F_1 = F_{11} + F_{12} + F_{13}$
$F_{11}$	Electron flow related to the one-electron photoreduction of $O_2^-$	$F_1 - 2k_{12}[NADP^+] - k_{13}[MDA]$
$F_{12}$	Electron flow related to the two-electron photoreduction of $NADP^+$ to NADPH	$2k_{12}[NADP^+]$
$F_{13}$	Electron flow related to the one-electron reduction of MDA to ASC	$k_{13}[MDA]$
$F_N$	NADPH flow related to the Calvin cycle	$k'_N[CO_2][NADPH]$
$F_5$	Rate of de novo synthesis of APX	$k_5^{APX}([APX]_0 - [APX] - [CoI] - [CoII])$

spontaneous dismutation (Bowler et al., 1992). In almost all plants, chloroplasts contain CuZn-SOD as the major isoform of the enzyme (Asada, 1999). These enzymes are known as superefficient  $O_2^-$  scavengers with pseudo first-order ( $k_{cat}/K_m$ ) catalytic rates as high as  $2 \times 10^9 M^{-1} s^{-1}$  in water and  $2 \times 10^8 M^{-1} s^{-1}$  in the stroma, owing to its high viscosity (Ogawa et al., 1995). Taking this into account and the fact that  $[O_2^-]$  inside chloroplasts is on the order of micromolar, first-order kinetics can be assumed for the rate of SOD with respect to  $[O_2^-]$ . So the following rate equation was used in our model:

$$V_{SOD} = k_{SOD}[SOD]_0[O_2^-] \quad (1)$$

## APX

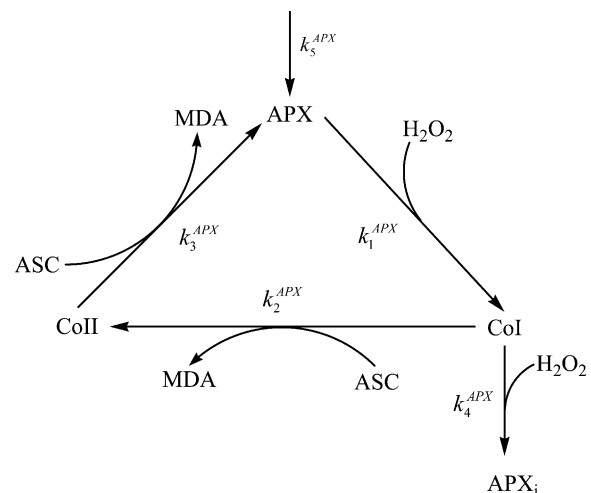
The  $H_2O_2$  produced via the SOD-catalyzed disproportionation of  $O_2^-$  is reduced to water by ASC, catalyzed with APX. This enzyme is a class I heme peroxidase (Welinder, 1992) whose catalytic mechanism is reminiscent of that observed in other peroxidases and involves the formation of an oxidized compound I (CoI) intermediate, which is subsequently reduced by substrate in two sequential, single-electron-transfer steps (Fig. 2). A characteristic property of APX, especially of the chloroplastic isoform, is its lability in the absence of its electron donor ASC (Miyake et al., 2006), since it is inactivated by the interaction of CoI with  $H_2O_2$ . To account for this fact, the step has been included in the catalytic cycle of the enzyme, along with a step corresponding to the de novo synthesis of APX. This last step must be included in the mechanism for the APX activity to attain the steady-state rate under nonstress conditions. The rate of the biosynthetic route ( $F_5$ ) is considered directly proportional to the amount of initial enzyme present in a nonactive form (Table I). So, at  $t = 0$ ,  $[APX] = [APX]_0$ ,  $[CoI] = [CoII] = [APX_i] = 0$ , and then  $F_5$  becomes  $F_5 = k_5^{APX}(0) = 0$  (i.e. the biosynthetic route does not work at  $t = 0$  since there is no inactive enzyme present). The more APX in the inactive form, the higher the term  $([APX]_0 - [APX] - [CoI] - [CoII])$ , so the rate of the biosynthetic route increases as the amount of active enzyme decreases. It is evident that the de novo synthesis in vivo is largely controlled by many factors other than APX, but we have chosen a simplified formula, since it is not possible to take into account all of these factors in the computer simulation. However, this fact does not change the general concept of our

model. Taking into account the complexity of the APX mechanism and the great interest in simulating its kinetic behavior at the physiological level, it has been included in full in the model (Supplemental Equations S9–S12).

MDA is the primary product of the APX-catalyzed reduction of  $H_2O_2$  by ASC, whose recovery is essential for maintaining the activity of the ROS-scavenging system. MDA spontaneously disproportionates to dehydroascorbate (DHA) and ASC in a pH-dependent way (Bielski et al., 1971). It is also directly reduced to ASC by photoreduced ferredoxin (redFd) in thylakoids (Miyake and Asada, 1994). The redFd competes between MDA and  $NADP^+$ , but the reduction rate of MDA is 34-fold higher than that of  $NADP^+$  (Miyake and Asada, 1994; Asada, 1999). Thus, redFd is preferably used to reduce MDA rather than  $NADP^+$ , suggesting that MDA is mainly photoreduced via Fd but not via NAD(P)H with MDAR, at least in the thylakoidal scavenging system. Taking this into account, MDAR is not included in the present model, which does not change the general concept of our model.

## DHAR

This enzyme catalyzes the reduction of DHA to ASC, with GSH as the electron donor, in a ter bi reaction. The



**Figure 2.** APX mechanism introduced in the model, including the inactivation of the enzyme by reaction of CoI with  $H_2O_2$  and a continuous input of APX into the system by the de novo synthesis of the protein.  $APX_i$  is the inactive enzyme.

regeneration of ASC from DHA by GSH also occurs spontaneously, but the rate is too slow to account for the observed photoreduction of DHA in chloroplasts (Asada, 1999). Kinetic analysis of the enzymatic reaction (Shimaoka et al., 2003) suggested that the reaction proceeds by means of a bi uni uni ping-pong mechanism (Segel, 1975), in which the binding of DHA to the free, reduced form of the enzyme was followed by the binding of GSH. Solving the ODE system corresponding to this mechanism for the forward reaction leads to the following rate equation under steady-state conditions, which has been used in our model:

$$V_{\text{DHAR}} = \frac{k_{\text{cat}}^{\text{DHAR}} [\text{DHAR}]_0 [\text{DHA}] [\text{GSH}]}{K_i^{\text{DHA}} K_m^{\text{GSH1}} + K_m^{\text{DHA}} [\text{GSH}] + (K_m^{\text{GSH1}} + K_m^{\text{GSH2}}) [\text{DHA}] + [\text{DHA}] [\text{GSH}]} \quad (2)$$

This equation contains an independent term in the denominator,  $K_i^{\text{DHA}} K_m^{\text{GSH1}}$ , which we have grouped as  $K$ . The first expression,  $K_i^{\text{DHA}}$ , is the equilibrium constant between DHA, DHAR, and the enzyme-substrate DHAR-DHA complex.  $K_m^{\text{GSH1}}$  and  $K_m^{\text{GSH2}}$  are the values of  $K_m$  for the first-binding and the second-binding molecules of GSH, respectively. The sum  $K_m^{\text{GSH1}} + K_m^{\text{GSH2}}$  has also been grouped as  $K_m^{\text{GSH}}$  in our model, since it has not been possible to calculate these values separately in kinetic assays (Shimaoka et al., 2003).

Note that Equation 2 can be simplified to the following expression:

$$V_{\text{DHAR}} = k_{\text{DHAR}} [\text{DHAR}]_0 [\text{DHA}] [\text{GSH}] \quad (3)$$

when the following condition is fulfilled:

$$K \gg K_m^{\text{DHA}} [\text{GSH}] + K_m^{\text{GSH}} [\text{DHA}] + [\text{DHA}] [\text{GSH}] \quad (4)$$

being:

$$k_{\text{DHAR}} = \frac{k_{\text{cat}}^{\text{DHAR}}}{K} \quad (5)$$

## GR

The supply of GSH is regenerated in an NADPH-dependent reaction catalyzed by GR. Kinetic studies performed with this enzyme have revealed a bi ter ping-pong mechanism (Vanoni et al., 1990). The rate equation corresponding to this mechanism under steady-state conditions for the forward reaction is the following, used in our model:

$$V_{\text{GR}} = \frac{k_{\text{cat}}^{\text{GR}} [\text{GR}]_0 [\text{NADPH}] [\text{GSSG}]}{K_M^{\text{NADPH}} [\text{GSSG}] + K_M^{\text{GSSG}} [\text{NADPH}] + [\text{NADPH}] [\text{GSSG}]} \quad (6)$$

## Other Steps Involved in the Model

An additional route of NADPH consumption by the Calvin cycle (and other electron-consuming reactions) has also been added to the model, although in a simplified way, as a flux with an apparent rate constant,  $k_N = k'_N [\text{CO}_2]$ . Other nonenzymatic reactions participating in the cycle and included in our model are indicated in Figure 1.

The ODE system that describes the mechanism shown in Figure 1 is shown in the supplemental data. The values for the kinetic constants and the initial conditions used to run the model are listed in Tables II and III, respectively. The rate constants corresponding to spontaneous steps are apparent bimolecular rate constants. Values for the kinetic parameters involved in the model have been taken from Asada (1999), Polle (2001), or from references describing kinetic studies of the target reaction. Other numerical values used were arbitrary but chosen to furnish reasonable data.

## RESULTS

### Kinetic Behavior of the GSH-ASC Cycle as a Substrate Cycle

At the enzymatic level (i.e. without considering any spontaneous steps involved in the cycle or the electron

**Table II.** Kinetic constants used to run the present model

Kinetic Constant	Value	Unit	Reference
$F_1$	640	$\mu\text{M s}^{-1}$	Polle (2001)
$k_{\text{cat}}^{\text{GR}}$	595	$\text{s}^{-1}$	Polle (2001)
$k_{\text{cat}}^{\text{DHAR}}$	142	$\text{s}^{-1}$	Polle (2001)
$k_{\text{SOD}}^{\text{APX}}$	200	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada (1999)
$k_1^{\text{APX}}$	12	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada (1999)
$k_2^{\text{APX}}$	50	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada (1999)
$k_3^{\text{APX}}$	2.1	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada (1999)
$k_4^{\text{APX}}$	0.7	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada (1999)
$k_5^{\text{APX}}$	0.01	$\text{s}^{-1}$	–
$k_3$	0.5 (pH 7.0)	$\mu\text{M}^{-1} \text{s}^{-1}$	Bielski et al. (1971)
$k_4$	0.1	$\mu\text{M}^{-1} \text{s}^{-1}$	Hausladen and Kunert (1990)
$k_5$	0.2 (pH 7.0)	$\mu\text{M}^{-1} \text{s}^{-1}$	Fridovich (1998)
$k_6$	0.2	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada and Takahashi (1987)
$k_7$	0.7	$\mu\text{M}^{-1} \text{s}^{-1}$	Asada and Takahashi (1987)
$k_8$	$2.0 \times 10^{-6}$	$\mu\text{M}^{-1} \text{s}^{-1}$	Polle and Junkermann (1996)
$k_{12}$	1.3	$\text{s}^{-1}$	–
$k_{13}$	42.5	$\text{s}^{-1}$	–
$k_N = k'_N [\text{CO}_2]$	0.5	$\text{s}^{-1}$	–
$K_m^{\text{NADPH}}$	3	$\mu\text{M}$	Polle (2001)
$K_m^{\text{GSSG}}$	$2.0 \times 10^2$	$\mu\text{M}$	Polle (2001)
$K_m^{\text{DHA}}$	70	$\mu\text{M}$	Polle (2001)
$K_m^{\text{GSH}}$	$2.5 \times 10^3$	$\mu\text{M}$	Polle (2001)
$K$	$5.0 \times 10^5$	$\mu\text{M}^2$	–

**Table III.** Initial concentrations used to run the model

These values were chosen to be similar to those used by Polle (2001), although we have preferred the system to synthesize  $O_2^-$  and  $H_2O_2$  by itself at the beginning of the reaction as a function of the initial conditions. The initial concentrations of  $O_2^-$ ,  $H_2O_2$ , and other species, therefore, were set to zero.

Species	Initial Concentration
	$\mu M$
GR	1.4
DHAR	1.7
SOD	50
APX	70
NADPH	150
GSH	4,000
ASC	10,000

source from PSI, except for the spontaneous dismutation of the MDA necessary for DHAR), the GSH-ASC cycle can be seen as two coupled substrate cycles involving the participation of APX, DHAR, and GR (Fig. 1, boldface steps). Substrate cycles are powerful metabolic tools involving two enzymes acting in opposite directions, whereby a target metabolite is reversibly interconverted into another chemical species without being consumed (Newsholme et al., 1984; Valero and García-Carmona, 1996; Valero et al., 2000). This is accompanied by the concomitant accumulation of other noncycling products at each turn of the cycle. The physiological explanation proposed for this wasteful cycling is that it is mainly a way of amplifying a metabolic response to a change in a metabolic concentration, thus greatly improving the sensitivity of metabolic regulation.

One of the main advantages of computer simulation is that it allows the dynamic behavior of a metabolic pathway to be studied by introducing the desired steps in the model until it is understood. The great amplification capacity of the GSH-ASC cycle can be checked by computer simulation of the boldface steps in Figure 1. The results obtained showed that an initial concentration of  $H_2O_2$  as high as  $10 \mu M$ , which has been reported to inhibit photosynthesis by 50% (Kaiser, 1979), was rapidly removed by the cyclic system in less than 0.02 s (half-time = 0.83 ms) at the expense of the equivalent consumption of NADPH.

When the spontaneous steps shown in Figure 1 were added to the model, the results obtained were very similar (data not shown), the most noteworthy differences being the lower accumulation of DHA in the first instants of the reaction, the shorter recovery time of the reducing species (GSH and ASC), an increased  $V_{GR}$  and a decreased  $V_{DHAR}$ . In contrast, if  $[GR]_0$ ,  $[DHAR]_0$ , and  $[APX]_0$  are made equal to zero and only spontaneous steps are operative in the system, the data obtained point to the slower removal of  $H_2O_2$  (half-time = 34.65 s) and low ASC recovery. GSH cannot recover simply by means of these spontaneous reactions.

### Kinetic Behavior of the System in Unstressed Chloroplasts

In the chloroplast, the cycle is not metabolically isolated; so now that we know how the cycle functions, we can introduce its immediate environment. Photo-reduction of molecular oxygen in the PSI of chloroplasts generates  $O_2^-$  continuously in daylight, which means that the  $H_2O_2$  must be continuously removed by the GSH-ASC cycle, for which the level of NADPH must recover. This process occurs in the photochemical phase of photosynthesis in PSI, although it is also important to take into account the consumption of NADPH in the Calvin cycle in the presence of  $CO_2$ . All of these steps, as well as the photoreduction of MDA, have been included in our model.

Unstressed chloroplasts generally show low, stationary levels of ROS and high ratios for the reduced form/oxidized form of the redox pairs involved in the cycle. The conditions indicated in Tables II and III have been chosen to mimic the behavior of the GSH-ASC cycle in unstressed chloroplasts. Under these conditions, a steady state was rapidly achieved by the system, in which metabolite concentrations and fluxes remained constant. The steady-state concentrations thus obtained were as follows:  $[NADPH]_{ss} = 84.95 \mu M$ ,  $[GSH]_{ss} = 3.98 \text{ mM}$ ,  $[ASC]_{ss} = 9.99 \text{ mM}$ ,  $[DHA]_{ss} = 42.9 \text{ nM}$ ,  $[MDA]_{ss} = 5.85 \mu M$ ,  $[O_2^-]_{ss} = 8.9 \text{ nM}$ , and  $[H_2O_2]_{ss} = 0.16 \mu M$ . These values are close to the ranges estimated for healthy tissues (Asada, 1994). The  $[MDA]_{ss}$  is a little high, perhaps because MDAR is not included in our model. However  $[DHA]_{ss}$  is very low in comparison with the levels usually found in plants (Polle, 1997; Kwon et al., 2003). Any inactivation of APX during integration time was negligible under these conditions, since ASC levels remained high throughout the reaction.

An  $O_2^-$  steady-state production rate of  $222.2 \mu M s^{-1}$  was obtained, which is within the range previously mentioned by other authors (Asada, 1999; Polle, 2001), while the conversion rate of MDA into ASC ( $248.7 \mu M s^{-1}$ ) was slightly higher and the photochemical recycling of NADPH ( $169.1 \mu M s^{-1}$ ) was slightly slower, reflecting the preference of redFd to reduce MDA rather than  $NADP^+$ . The most active enzymes were APX and SOD followed by GR and DHAR, since the low glutathione oxidized concentration ( $[GSSG]$ ) and  $[DHA]$  in these conditions limits their velocity. A maximum in  $V_{SOD}$  and  $V_{APX}$  was appreciated at the start of the reaction, since the enzymes must work hard to lower the accumulation of  $O_2^-$  and  $H_2O_2$ , respectively, in the initial phase (Supplemental Fig. S1).

### Kinetic Behavior of the System in Stressed Chloroplasts

Oxidative stress is characterized by the disruption of cellular homeostasis, leading to the enhanced production of ROS and changes in the redox state of chloroplasts. Many environmental perturbations, including intense light, temperature stress, air pollutants, and herbicides, affect the efficiency of photosynthetic electron transport. To study the dynamic behavior of the

system under these conditions,  $F_1$  was increased to  $2,450 \mu\text{M s}^{-1}$ . NADPH levels fell very rapidly in the first instants of the reaction, followed by GSH. ASC levels remained high as long as NADPH and GSH were present in the chloroplasts, although afterward they decreased sharply to reach limiting concentrations. The disappearance of ASC was followed by the rapid inactivation of APX, reflecting what occurs in reality (Miyake and Asada, 1996), accompanied by a sharp increase in  $[\text{APX}]_i$ . Once APX has been inactivated,  $\text{H}_2\text{O}_2$  is accumulated in the chloroplast at a very high rate, since it is continuously produced from  $\text{O}_2^-$ , spontaneously and enzymatically catalyzed by SOD. A minimum in  $[\text{MDA}]$  and in  $F_{13}$  could also be observed, after which  $[\text{MDA}]$  recovered by spontaneous steps. Consequently, a maximum in  $F_{11}$  and hence in  $[\text{O}_2^-]$  and  $V_{\text{SOD}}$  appeared. The increase in  $[\text{ASC}]$  once APX has been inactivated is due to the spontaneous redox steps involved in the model. However, it must be taken into account that all of these recoveries observed after APX inactivation are produced as a result of  $[\text{H}_2\text{O}_2]$  increasing above a life-compatible level, so they have no physical meaning.  $F_{12}$  and  $V_{\text{GR}}$  reached a steady state, which was not affected by APX inactivation.  $F_{\text{N}}$  sharply decreased near the start of the reaction as a consequence of NADPH depletion in the chloroplast (Supplemental Fig. S2).

### Kinetic Response of the System against an Increasing Electron Flux

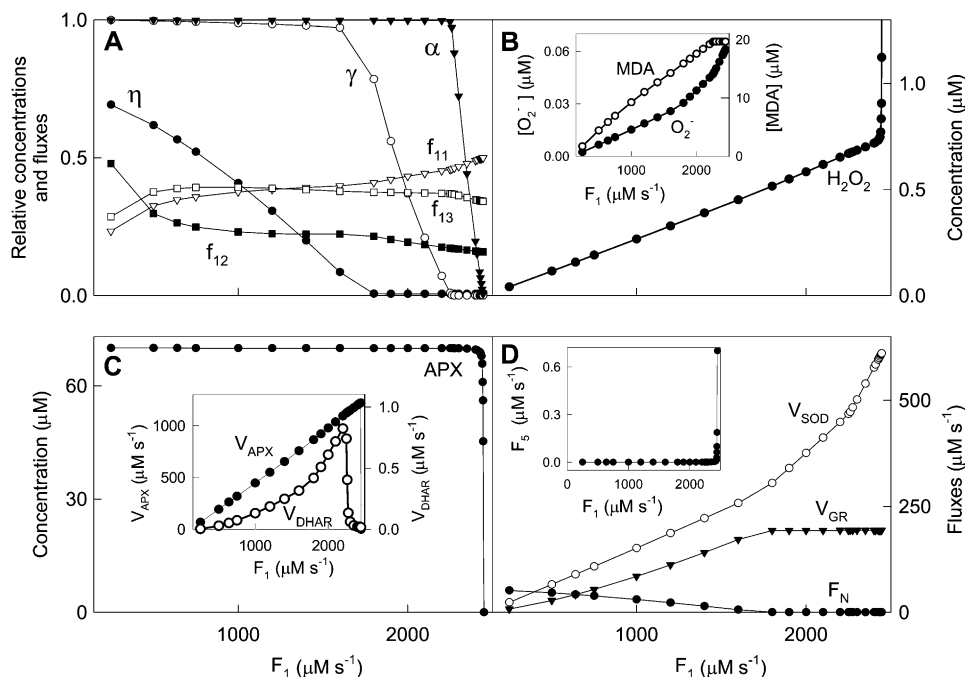
Intense light exposure causes oxidative stress in plants, but a high electron flux through the water-water cycle provides a way to dissipate excess light energy (Asada, 1999). To address the response of the system under study to this increasing oxidative stress,  $F_1$  was

varied from 250 to  $2,450 \mu\text{M s}^{-1}$  (i.e. until APX underwent photoinactivation by excess of  $\text{H}_2\text{O}_2$ ). Steady-state concentrations of metabolites involved in the mechanism under study and the fluxes thus obtained are shown in Figure 3. The model shows a progressive decrease in the steady-state levels of antioxidants as  $F_1$  increases, NADPH being the first to be depleted in the chloroplast, followed by GSH and ASC. The  $[\text{MDA}]_{\text{ss}}$ ,  $[\text{O}_2^-]_{\text{ss}}$ , and  $[\text{H}_2\text{O}_2]_{\text{ss}}$  increased linearly as long as  $F_1$  was low. At higher  $F_1$ ,  $[\text{MDA}]_{\text{ss}}$  remained constant, the accumulation of  $\text{O}_2^-$  was more pronounced (steeper slope of the plot), and  $[\text{H}_2\text{O}_2]_{\text{ss}}$  sharply increased owing to the induced photoinactivation of APX. APX falls in a very narrow range of  $F_1$  (Fig. 3C) when its inactivation exceeds its de novo synthesis, although its enzymatic activity continues increasing almost until the end, with the aim of eliminating as much  $\text{H}_2\text{O}_2$  as possible. The rate of de novo synthesis of APX ( $F_5$ ; Fig. 3D, inset) sharply increased with the inactivation of APX, which represents a defense against ROS.

The relative distribution of  $F_1$  among the three routes considered under these conditions is also shown in Figure 3A. It can be seen that at high  $F_1$ , only the  $\text{O}_2^-$  production rate increased.  $F_{\text{N}}$  decreased owing to the lower availability of NADPH (Fig. 3D), although  $V_{\text{GR}}$  increased steadily to reach a constant value because of increasing levels of GSSG in the chloroplast.  $V_{\text{SOD}}$  increased in a parallel way with  $[\text{O}_2^-]_{\text{ss}}$ , and  $V_{\text{DHAR}}$  showed a maximum, after which it abruptly fell, pointing to the next photoinactivation of APX.

### Effects on the System of Varying $k_{12}$ and $k_{13}$

The detoxifying efficiency of the mechanism under study is probably best evaluated by the relative dis-



**Figure 3.** Dependence of steady-state concentrations and fluxes on  $F_1$  variations. The values of the rate constants and initial conditions used were those shown in Tables II and III, except that  $F_1$  was varied between 250 and  $2,450 \mu\text{M s}^{-1}$ . Relative concentrations and fluxes are defined in "Materials and Methods."

tribution of  $F_1$  among the three competitive routes through the system. To do this, we have introduced a constant value of  $F_1 = 2,000 \mu\text{M s}^{-1}$ , and computer simulations were performed by varying  $k_{12}$  and  $k_{13}$ . The system is extremely sensitive to low values of  $k_{12}$  and  $k_{13}$  when the photochemical recovery of NADPH and ASC is inoperative and the photoproduction rate of  $\text{O}_2^-$  is higher (Figs. 4 and 5). For this reason, antioxidants were rapidly depleted and APX suffered inactivation in a very low range of  $k_{12}$  and  $k_{13}$ . Therefore, sharp increases in  $[\text{NADP}^+]_{\text{ss}}$ ,  $[\text{GSSG}]_{\text{ss}}$ ,  $[\text{DHA}]_{\text{ss}}$ ,  $[\text{O}_2^-]_{\text{ss}}$ , and  $[\text{H}_2\text{O}_2]_{\text{ss}}$  and increasing  $V_{\text{SOD}}$  and  $V_{\text{APX}}$  values are observed at low  $k_{12}$  and  $k_{13}$ . The MDA plot, however, shows a maximum at low  $k_{12}$ , which is related to APX photoinactivation when ASC concentration is limiting. This maximum in  $[\text{MDA}]_{\text{ss}}$  is not seen at low  $k_{13}$ , since the electron flux deviated by the  $F_{13}$  branch for the photorecycling of ASC continuously increases to reach a nearly constant value.

It is also possible to observe in Figure 4A an increase in  $F_{12}$  when  $k_{12}$  increased at low values, essentially at the expense of  $F_{11}$ . In contrast,  $F_{12}$  remained constant when  $k_{13}$  was increased at low values (Fig. 5A). In this last plot,  $F_{13}$  increased basically at the expense of  $F_{11}$ ; once  $F_{11}$  attained a nearly constant value,  $F_{13}$  continued increasing at the expense of  $F_{12}$ . Note that at higher  $k_{12}$  and  $k_{13}$  values, the distribution of the electron flux from PSI became almost constant (i.e. the system was saturated). Figures 4D and 5D show a similar dependence of  $F_{\text{N}}$  as  $k_{12}$  and  $k_{13}$  were increased, in agreement with the greater availability of NADPH. NADPH almost completely recovered at relatively high values of  $k_{12}$ , but not by increasing  $k_{13}$  under the conditions used here. The dependence of  $V_{\text{GR}}$  on  $k_{12}$  and  $k_{13}$  was parallel to its respective  $F_{12}$  plot, and a maximum in  $V_{\text{DHAR}}$  was

also obtained in both cases at low  $k_{12}$  and  $k_{13}$ , again pointing to the next photoinactivation of APX.

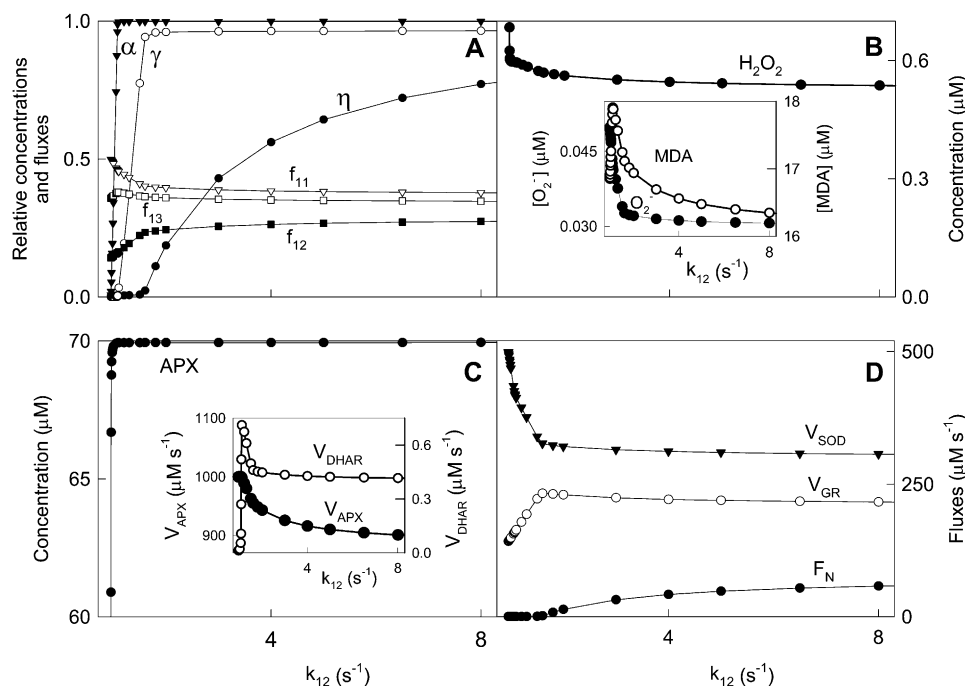
#### Effects on the System of Varying $k_{\text{N}}$

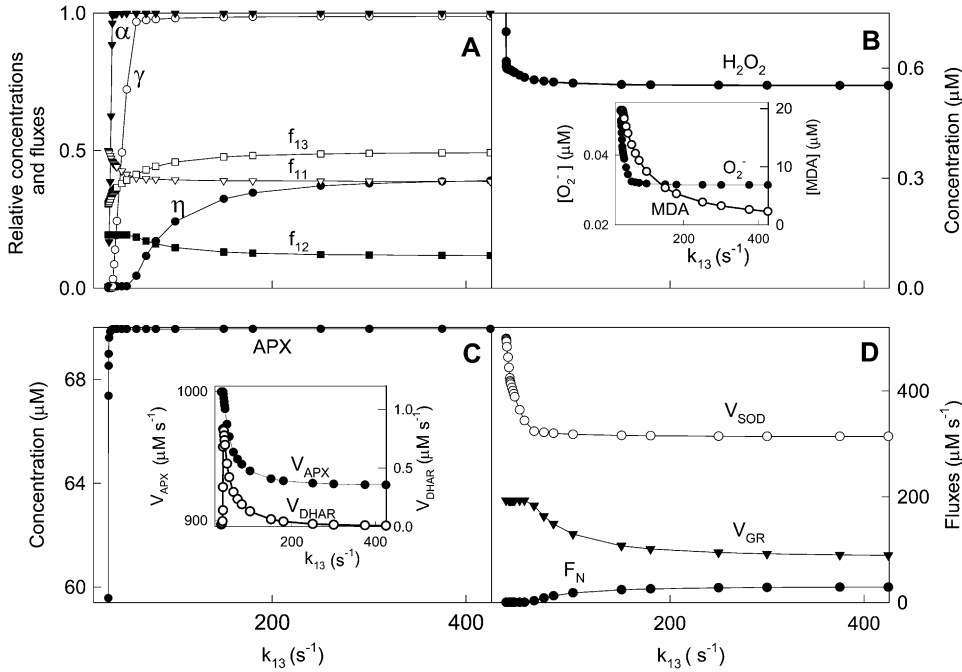
We have introduced the photoproduction of NADPH and its consumption during the  $\text{CO}_2$  fixation in a simplified way through the  $F_{\text{N}}$  flux step. Thus,  $k_{\text{N}}$  is a kinetic parameter related to the Calvin cycle and other electron-consuming reactions under conditions of constant  $[\text{CO}_2]$ . Computer simulations pointed to the great sensitivity of the model to the  $k_{12}/k_{\text{N}}$  ratio. Figure 6 shows the results obtained when varying  $k_{\text{N}}$  for a fixed value of  $k_{12} = 2 \text{ s}^{-1}$ . Minimums in  $[\text{O}_2^-]_{\text{ss}}$ ,  $V_{\text{SOD}}$ , and  $F_{11}$  can be seen at low  $k_{\text{N}}$ , meaning variations in  $k_{\text{N}}$  can lead to the system adapting to light intensity, giving rise to minimal ROS levels. Therefore, an appropriate Calvin cycle rate (e.g. by means of an adequate level of  $\text{CO}_2$ ) might provide protection against ROS.

As  $k_{\text{N}}$  was increased, the antioxidant concentration in the chloroplast gradually decreased, in the order NADPH, GSH, ASC, so that their respective oxidized species concentrations increased, although  $[\text{MDA}]_{\text{ss}}$  decreased due to the lower availability of ASC to spontaneously react with  $\text{O}_2^-$  to produce it.  $[\text{H}_2\text{O}_2]_{\text{ss}}$  showed a gradual decrease in spite of the increase in  $[\text{O}_2^-]_{\text{ss}}$  once NADPH was nearly depleted, which was probably related to spontaneous steps since  $[\text{APX}]_{\text{ss}}$  and its activity also decreased. Once ASC became limiting, APX was inactivated, so that  $[\text{H}_2\text{O}_2]$  increased abruptly.

With regard to the electron fluxes,  $F_{12}$  increased as long as NADPH was left in the chloroplast but remained nearly constant when NADPH was nearly depleted.  $F_{11}$  and  $F_{13}$  decreased at low  $k_{\text{N}}$  and after  $F_{11}$

**Figure 4.** Dependence of steady-state concentrations and fluxes on  $k_{12}$  variation. The values of the rate constants and initial conditions used were those shown in Tables II and III, except that  $F_1 = 2,000 \mu\text{M s}^{-1}$  and  $k_{12}$  was varied between 0.95 and  $250 \text{ s}^{-1}$ .





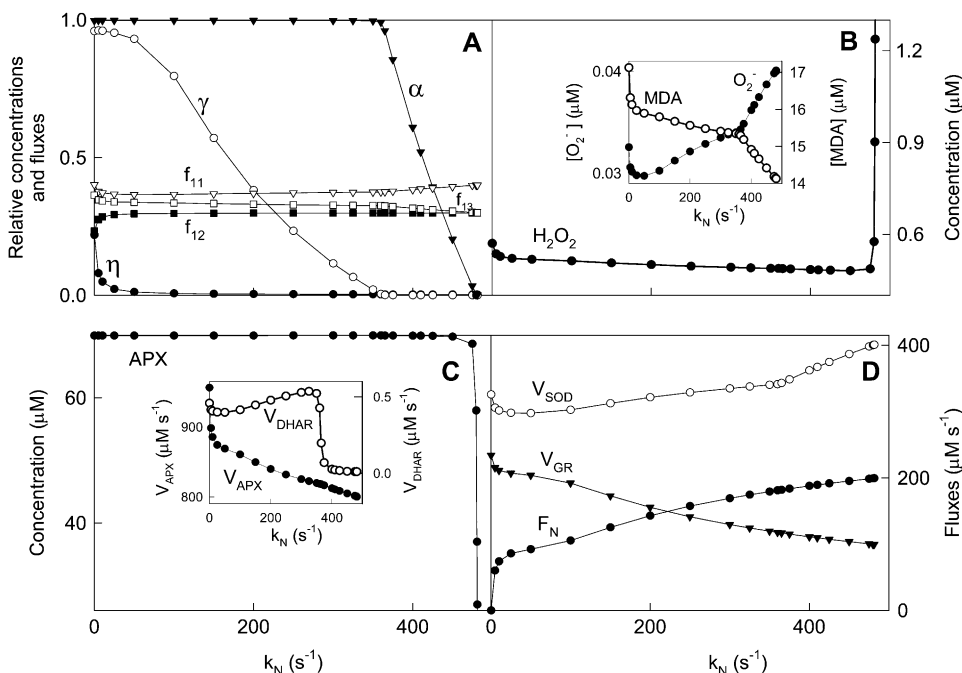
**Figure 5.** Dependence of steady-state concentrations and fluxes on  $k_{13}$  variation. The values of the rate constants and initial conditions used were those shown in Tables II and III, except that  $F_1 = 2,000 \mu\text{M s}^{-1}$  and  $k_{13}$  was varied between 31.1 and  $500 \text{ s}^{-1}$ .

increased at the expense of  $F_{13}$ . A maximum in  $V_{\text{DHAR}}$  prior to the photoinactivation of APX could be seen again.  $V_{\text{GR}}$  decreased with increasing  $k_N$  as a consequence of the lower availability of NADPH, whereas  $F_N$  evidently increased.

**Effects on the System of Varying Antioxidant Enzyme Concentrations**

Antioxidant enzymes are critical components in preventing oxidative stress in plants. Manipulation

of the expression of these enzymes by gene transfer technology has provided new insight into their role in chloroplasts by allowing direct investigation of their functions and interactions (Foyer et al., 1994; Allen et al., 1997). Mathematical modeling is also a powerful tool that can be used to predict the response of the system to changes in the activities and concentrations of the enzymes involved in the pathway. Therefore, computer simulations were performed here at different initial concentrations of the four enzymes considered in our model.



**Figure 6.** Dependence of steady-state concentrations and fluxes on  $k_N$  variation. The values of the rate constants and initial conditions used were those shown in Tables II and III, except that  $F_1 = 2,000 \mu\text{M s}^{-1}$ ,  $k_{12} = 2 \text{ s}^{-1}$ , and  $k_N$  was varied between 0 and  $487 \text{ s}^{-1}$ .



Decreasing levels of  $[GR]_0$  (data not shown) led to the irreversible photoinactivation of APX, again announced by a maximum in  $V_{DHAR}$ , resulting in considerable increases in  $[GSSG]_{ss}$ ,  $[DHA]_{ss}$ ,  $[H_2O_2]_{ss}$ , and  $[O_2^-]_{ss}$ , accompanied by increases in  $F_{11}$ ,  $V_{SOD}$ , and  $V_{APX}$ . However, NADPH consumption was lower at low  $[GR]_0$ , and an increase in  $F_N$  was observed.

It has been reported that plants overexpressing GR are more tolerant of ROS-inducing herbicides such as methyl viologen, since they are able to maintain the reduction state of their ascorbate pools more effectively than control plants (Aono et al., 1991; Foyer et al., 1991). The numerical data obtained here agree with these results. Increasing levels of  $[GR]_0$  led to the recovery of ASC and APX and the partial recovery of GSH, although NADPH decreased due to its greater consumption by GR. In the same way,  $[GSSG]_{ss}$ ,  $[DHA]_{ss}$ ,  $[H_2O_2]_{ss}$ , and  $[O_2^-]_{ss}$  decreased to reach nearly constant values.  $[MDA]_{ss}$  showed a maximum at low  $[GR]_0$ , and also reached a nearly constant value when  $[GR]_0$  increased.  $F_{12}$  and  $F_{13}$  increased at low  $[GR]_0$  as a consequence of the decrease in  $F_{11}$ , while  $V_{GR}$  only increased at low  $[GR]_0$ , also reaching a nearly constant value.

Unlike changes in  $[GR]_0$ , variations in  $[DHAR]_0$  in our model had no noticeable effect on the steady-state concentrations of metabolites or on the fluxes through the GSH-ASC pathway (data not shown), even when  $[DHAR]_0 = 0$ . Only a very slight decrease in  $[DHA]_{ss}$  accompanied by a slight increase in  $[ASC]_{ss}$  could be observed as  $[DHAR]_0$  increased, with a subsequent decrease in the rate of the spontaneous reaction between GSH and DHA. This means that this spontaneous step could be sufficient to cope with DHA removal, as suggested by Polle (2001). However, these results must be interpreted in the context of the present model, and they do not mean that DHAR is a dispensable enzyme in reality, in agreement with data reported by Chen and Gallie (2006). When computer simulations were performed in the absence of spontaneous DHA reduction ( $k_4 = 0$ ), a threshold  $[DHAR]_0$  was necessary if ASC levels were to recover and to prevent APX inactivation. It was also observed that under these conditions,  $V_{DHAR}$  was higher than usually observed when  $k_4 \neq 0$ .

When  $[APX]_0$  was increased, a threshold value of  $[APX]_0$  of  $3.37 \mu M$  was found to be necessary for the system to reach a steady state. Below this value, APX was irreversibly inactivated, since insufficient protein was supplied by de novo synthesis, and consequently,  $[H_2O_2]$  increased to toxic amounts. However, no appreciable effects on the steady state of the antioxidant pools,  $[MDA]_{ss}$ , and  $[O_2^-]_{ss}$  or on the fluxes and velocities of the other enzymes involved in the system were observed, even when  $[APX]_0 = 0$  (data not shown). These results indicate that high  $[H_2O_2]$  might coexist with high  $[GSH]$  and  $[ASC]$ , although they should be treated with caution, since other possible pernicious effects of  $H_2O_2$  in the cell have not been included in the model. Above the previously mentioned threshold value of  $[APX]_0$ , the

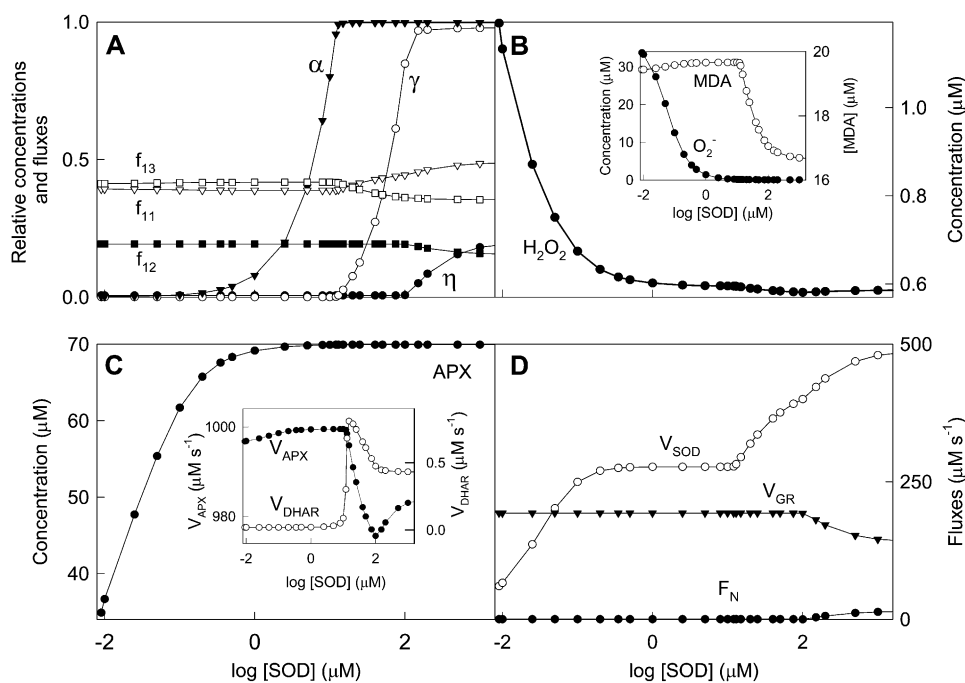
plots remained constant and parallel to the abscissa axis, the only changes observed being a decrease in  $[H_2O_2]_{ss}$ , an increase in  $[APX]_{ss}$ , and a rapid increase in  $V_{APX}$  until it reached a constant value.

When  $k_5^{APX}$  (the apparent rate constant for the de novo synthesis of APX) was increased from  $0.01$  to  $1 s^{-1}$ , the system showed greater tolerance against oxidative stress conditions and the inactivation of the peroxidase enzyme was less abrupt (data not shown). This result agrees with the experimentally observed increased tolerance to methyl viologen damage reported in tobacco (*Nicotiana tabacum*) plants overexpressing cytosolic APX (Pitcher et al., 1994), although it is in apparent contradiction with data obtained by the same authors (Torsethaugen et al., 1997), indicating that overproduction of APX in tobacco chloroplasts does not provide protection against  $O_3$ -induced stress. This may be due to the above-mentioned fact that  $V_{APX}$  remained nearly constant above a certain value (about  $10 \mu M$  under the conditions used here) even when the  $[APX]$  was increased.

Finally,  $[SOD]_0$  was varied from  $9 nM$  to  $1 mM$  (Fig. 7). A value of less than  $9 nM$  led to depletion of antioxidants, the inactivation of APX, and an excessive accumulation of  $H_2O_2$  even if  $[SOD]_0 = 0$ . However  $O_2^-$  was not accumulated, since most of the  $O_2^-$  photo-generated in the chloroplast disappeared through spontaneous dismutation and reaction with ASC and GSH, yielding  $H_2O_2$ .

Computer simulations performed at low values of  $[SOD]_0$  yielded increased levels of  $NADP^+$ , GSSG, DHA, MDA,  $H_2O_2$ , and  $O_2^-$ , indicating that a certain level of SOD is necessary for the plant to maintain its reduction potential against oxidative stress. These responses of the system disappeared when  $[SOD]_0$  was increased, since GSH levels began to recover and ASC was almost totally recovered. The inactivation of APX was negligible under these conditions, and  $[MDA]_{ss}$ ,  $[O_2^-]_{ss}$ ,  $[H_2O_2]_{ss}$ , and  $V_{APX}$  decreased as a consequence of the lower amount of  $H_2O_2$  accumulated. Again, a maximum in  $V_{DHAR}$  appeared. The increase in  $F_{11}$  was accompanied by an increase in  $V_{SOD}$ . This illustrates the balance between  $O_2^-$  production and elimination in the metabolism. That is, when the chloroplast has insufficient  $O_2^-$  because of an excess of SOD (or for any other reason), part of the electron flux from PSI is directed to the production of more  $O_2^-$ , so that ASC and NADPH photochemical recovery fall.

These data demonstrate that SOD is a critical component of the ROS-scavenging system of chloroplasts and indicate that overexpression of this enzyme in transgenic plants may improve plant stress tolerance. Transgenic plants with high levels of the three types of SOD have been developed and characterized by several research groups. The results obtained showed that, in many cases, high levels of SOD in a variety of cellular compartments lead to detectable increases in cellular protection from oxidative stress (Allen et al., 1997), in agreement with the theoretical data obtained here.



**Figure 7.** Dependence of steady-state concentrations and fluxes on  $[SOD]_0$ . The values of the rate constants and initial conditions used were those shown in Tables II and III, except that  $F_1 = 2,000 \mu\text{M s}^{-1}$  and  $[SOD]_0$  was varied between 9 nM and 1 mM.

## DISCUSSION

A new mathematical model has been developed for the kinetic study of the complex network of redox reactions involved in the GSH-ASC pathway for detoxifying ROS in chloroplasts. The model is based on another one reported previously by Polle (2001), although we have included several modifications that considerably improve it, bringing the results obtained nearer to reality.

We have introduced into the model the ODE corresponding to NADPH and  $\text{NADP}^+$ , taking into account the balance between the photochemical recovery of NADPH, its consumption by the Calvin cycle, and the GR-catalyzed reaction. Polle's model (2001) could not contemplate this important subject from a physiological point of view because of excessive run times in the computer, so the corresponding equations were simplified. The consequence was that NADPH could not be recovered (it was assumed as a constant value), leading to the continuous accumulation of  $\text{NADP}^+$  in the chloroplast. However, as shown here,  $\text{H}_2\text{O}_2$  is detoxified at the expense of the reducing power of NADPH. In its evolution since the appearance of oxygen in the atmosphere, the cell has developed a very efficient defense tool against oxygen toxicity, based on two coupled substrate cycles, although it needs a supply of NADPH. The waste of NADPH can be understood as the cost that chloroplasts must pay to swiftly detoxify  $\text{H}_2\text{O}_2$ . The present model is able to simulate this.

The pathway under study is very interesting, since the same daylight that gives rise to the synthesis of  $\text{O}_2^-$  toxic radicals also generates NADPH and ASC to detoxify the  $\text{H}_2\text{O}_2$  arising from  $\text{O}_2^-$  dismutation. Therefore, it is very important to know the relative

weight of each route in the growth conditions of the plant. This is taken into account in the present model by introducing a constant electron flux from PSI distributed among three competitive branches: the photoproduction of  $\text{O}_2^-$ , the photoreduction of  $\text{NADP}^+$ , and the photoreduction of MDA. Electron fluxes through these routes must adjust to each other as a function of the growth conditions of the plant. The fit between the three branches is a better way to understand the kinetic behavior of the pathway and the physiological response of chloroplasts in the face of a given stimulus, as has been shown by means of the computer simulations performed here.

Each enzyme involved in our model has been introduced into the ODE, taking into account its particular catalytic mechanism. This is especially important in the case of APX, since it is the most  $\text{H}_2\text{O}_2$  sensitive. SOD, DHAR, and GR are also inactivated, but only after long illumination in the presence of paraquat (Iturbe-Ormaetxe et al., 1998). Polle's model (2001) did not take into account the photoinactivation of APX, so a steady state was always attained. Instead, in our model, a steady state is only attained under nonstress conditions, when reducing power in the chloroplast is high and APX is not inactivated. The introduction of a step corresponding to the de novo synthesis of APX plays a double role in the model: on the one hand, it is necessary so that the system can reach a steady state under nonstress conditions; on the other hand, the results obtained are more realistic, since this is one of the main defense mechanisms of plants to mitigate oxidative stress. The present model is able to predict the rapid biosynthesis of the protein in response to harsh oxidative stress conditions.

The electron flux in the thylakoids also supplies NADPH for the Calvin cycle, so we included this in our model. There is a competition between the NADPH consumed by the ROS-detoxifying pathway and the NADPH consumed by the Calvin cycle. The results obtained here illustrate the importance of the fine regulation of the cycle, since the plots show a minimum of ROS production at low values of the apparent rate constant for the Calvin cycle ( $k_N$ ; Fig. 6B, inset). It is known that plants can regulate temporary mechanisms of stomatal closure in response to abiotic stress, thus limiting the entrance of CO<sub>2</sub> into chloroplasts and decreasing the amount of NADPH consumed by the Calvin cycle (Fig. 6D). The model developed here is able to simulate, to our knowledge for the first time, this interesting physiological response of plants and therefore should contribute to its better understanding.

## CONCLUSION

In conclusion, the mathematical model developed here is a very powerful tool for improving our theoretical understanding of the kinetic behavior of the ROS-detoxifying pathway in chloroplasts. The model, besides including new physiologically important aspects, such as the balance between the photogeneration and consumption of NADPH and APX inactivation, can easily be expanded to include new steps, such as regulatory devices for enzymes, dark-light interactions, the peroxiredoxin system (Dietz, 2003; Dietz et al., 2006), etc. It may also allow the guidance of future experimental work to evaluate those parameters involved in the cycle that have not been evaluated yet. In this way, the approach offers a new strategy for studying plant defense mechanisms against oxidative stress and can be used to predict the response of the plant to different stress conditions and where the limits of resistance can be expected.

## MATERIALS AND METHODS

Simulated progress curves were obtained by numerical solution of the nonlinear set of differential equations corresponding to the mechanism shown in Figure 1 (Supplemental Equations S1–S13). Numerical integration was performed using the `ode15s` function from MATLAB software version 7.0 (<http://www.mathworks.com>). This is a variable-order solver based on numerical differentiation formulas and is a multistep solver recommended for stiff problems (Shampine and Reichelt, 1997). The file including the ODE and the kinetic constant values used is available to interested readers on request. Fluxes and enzymatic activities were calculated from data thus obtained by a computer program made by us using the Transform tool in the SigmaPlot scientific graphing system for Windows version 8.02 (<http://www.spss.com>), which is also available to interested readers on request. Data thus obtained were plotted using the same software. Steady-state values for metabolite concentrations and fluxes plotted in Figures 3 to 7 were obtained from the linear portion of progress curves given by the computer. The points represent theoretical data obtained in the computer, and the solid lines are straight lines linking them. Relative concentrations of antioxidants were defined as follows:  $\alpha = [ASC]/[ASC]_0$ ,  $\gamma = [GSH]/[GSH]_0$ , and  $\eta = [NADPH]/[NADPH]_0$ . Relative fluxes were defined as follows:  $f_{11} = F_{11}/F_1$ ,  $f_{12} = F_{12}/F_1$ , and  $f_{13} = F_{13}/F_1$ .

These programs were run on a PC-compatible computer based on a Pentium IV 2-GHz processor with 512 MB of RAM. The time consumed by this

computer to obtain each particular numerical solution was on the order of a few seconds or even less in those cases in which a steady state was reached.

## Supplemental Data

The following materials are available in the online version of this article.

**Supplemental Figure S1.** Simulated progress curves corresponding to the species involved in the mechanism shown in Figure 1, in unstressed chloroplasts.

**Supplemental Figure S2.** Simulated progress curves corresponding to the species involved in the mechanism shown in Figure 1, in stressed chloroplasts.

**Supplemental Equations S1 to S13.** Differential equations system corresponding to the mechanism shown in Figure 1.

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